



EUROPEAN ROBOTICS FORUM 2017, 2017-03-23

# You cannot measure everything

On the importance of models for estimation in robotics

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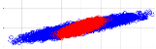
# You cannot measure everything – Overview



Increasing importance of models



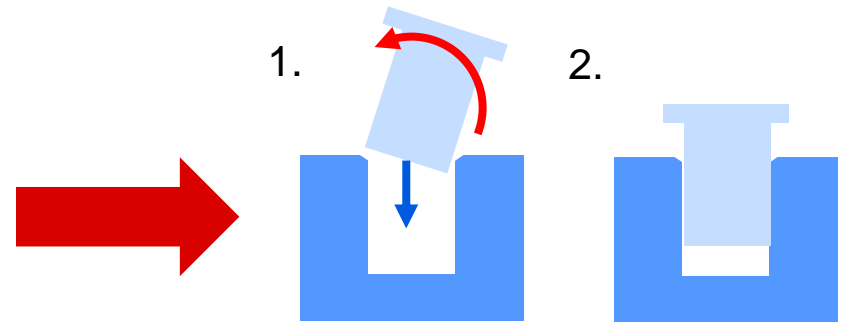
Models for joint load torque estimation



Models for Cartesian contact force estimation

# Increasing importance of models in robotics

New applications



Pure motion control → Combined force/motion control

# Increasing importance of models in robotics

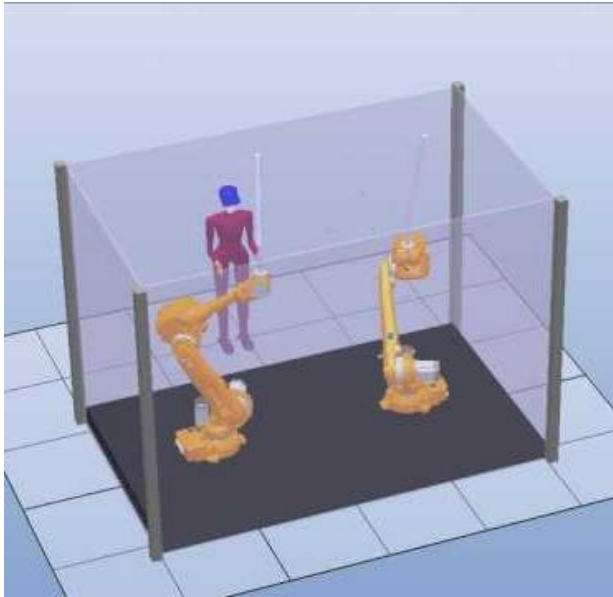
New robot designs



Lightweight designs → Reduced stiffness

# Increasing importance of models in robotics

Human-robot collaboration



HRC → Additional robot & human models

# Cartesian Contact Force Estimation

## Estimating joint load torques

Rigid manipulator  $M\ddot{q} + C\dot{q} + G + \tau_{fric} + \tau_{ext} = \tau_{mot}$

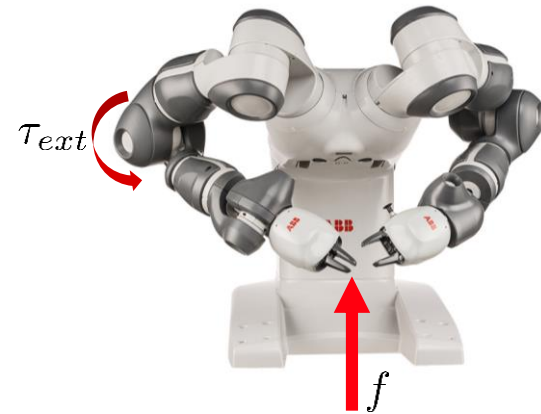
Assuming contact solely at TCP  $\tau_{ext} = J^T f$

### Simple load torque estimation

$$\hat{\tau}_{ext} = \tau_{mot} - \tau_{fric} - (M\ddot{q} + C\dot{q} + G)$$

Can be measured

Model needed



Assume  $\hat{\tau}_{ext} = \tau_{ext} + e_j$ ,  $e_j \sim \mathcal{N}(0, \Sigma_j)$

$$\Sigma_f(q) = W(q) \cdot \Sigma_j \cdot W(q)^T$$

Uncertainty in Cartesian space

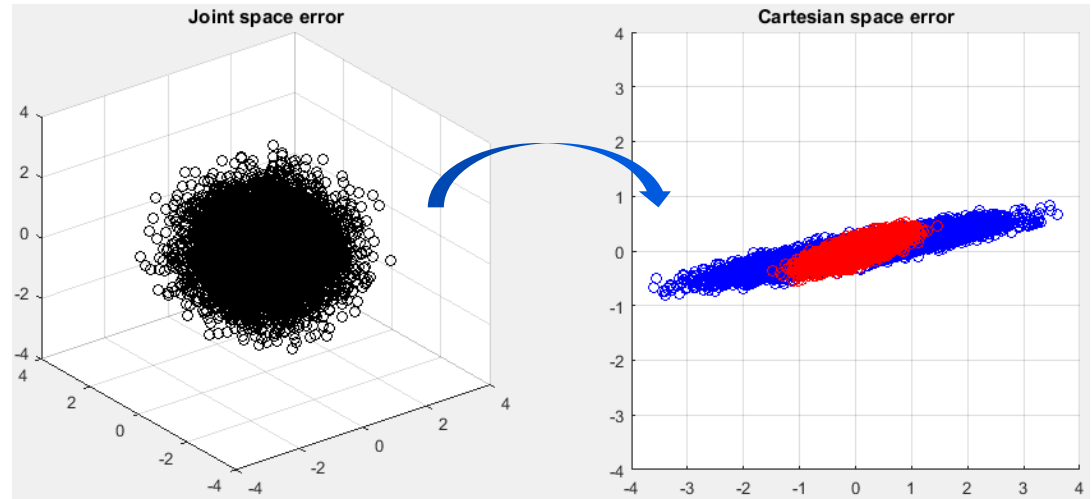
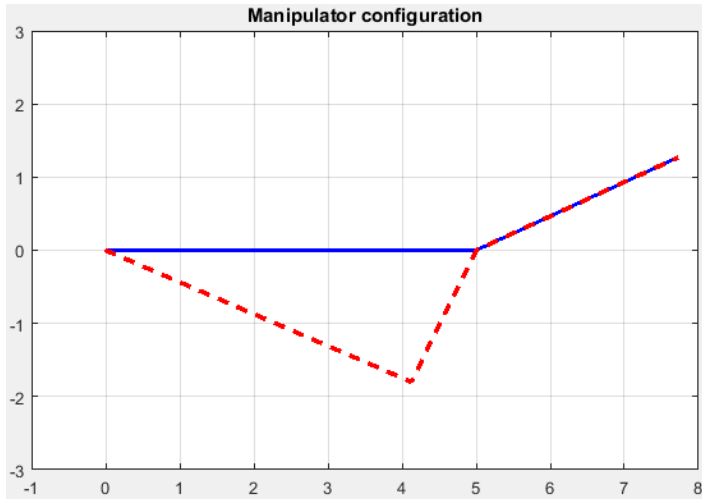
$$\hat{f} = W \hat{\tau}_{ext} = (J^T)^{-1} \hat{\tau}_{ext}$$

# Cartesian Contact Force Estimation

Mapping joint load torques to Cartesian space

Mapping from joint space to Cartesian space – Redundant case

$$\hat{f} = (J^T)^+ \hat{\tau}_{ext}$$



Reduced variance in Cartesian space

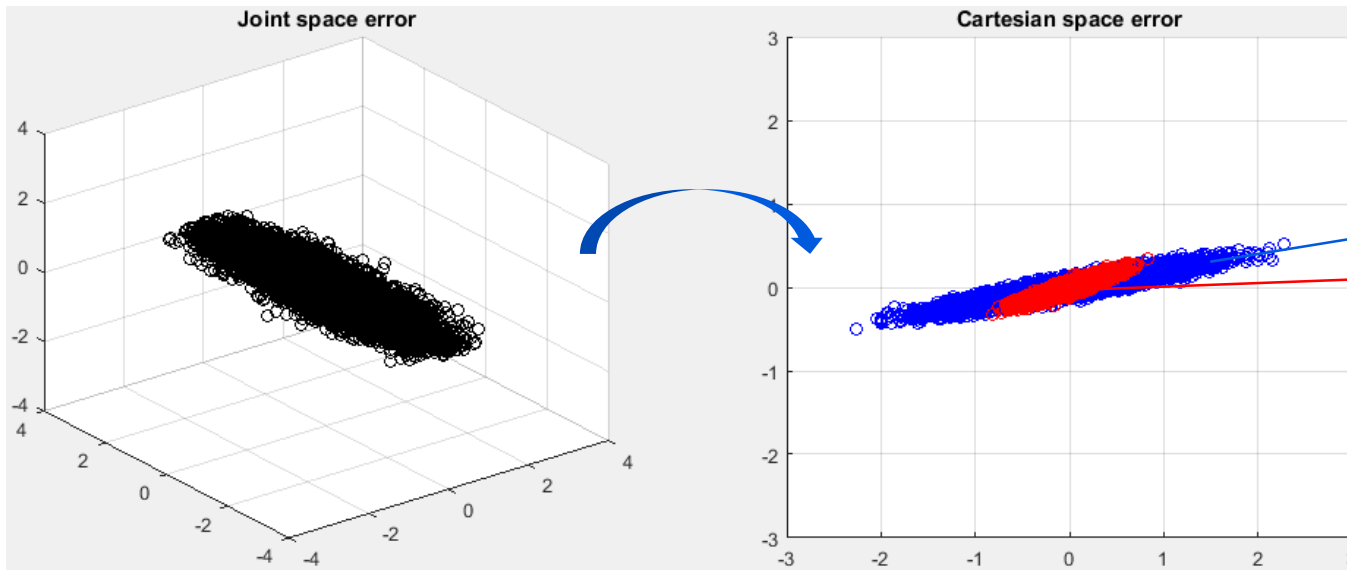
More information → Better results

# Cartesian Contact Force Estimation

## Mapping joint load torques to Cartesian space

Exploiting prior knowledge on joint level uncertainty  $\Sigma_j \neq I$

$$\text{Maximum likelihood estimator } \hat{f} = \underbrace{(J \cdot \Sigma_j^{-1} \cdot J^T)^{-1} \cdot J \cdot \Sigma_j^{-1}}_{W = (J^T)_{\Sigma_j}^{\#}} \cdot \hat{\tau}_{ext}$$



Example:

$$\Sigma_j = \text{diag}(0.4; 1.6; 0.1)$$

$$(J^T)^+$$

$$(J^T)_{\Sigma_j}^{\#}$$

Confidence information  
→ Better results



# Cartesian Contact Force Estimation

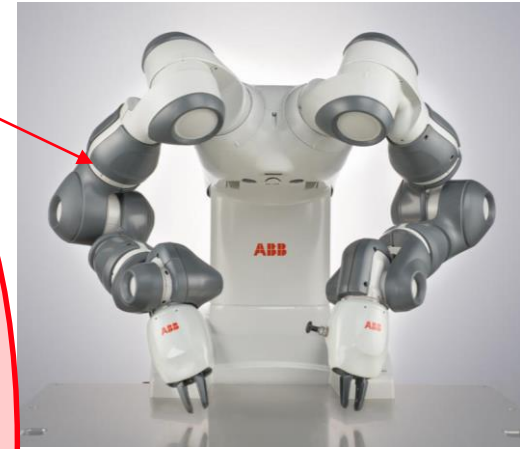
Mapping joint load torques to Cartesian space

(Artificial) YuMi example:  $J(q) \in \mathbb{R}^{6 \times 7}$ ,  $\Sigma_j = \text{diag}(1; 1; 1; 1; 1; 1; 100)$

Joint load torque estimation  
much worse on J7

$$(J^T)^+ = \begin{bmatrix} 2.35 & 1.63 & -5.73 & 0.01 & 3.12 & 0.44 & 0.63 \\ 2.78 & -0.15 & -1.80 & -0.88 & -0.77 & -0.86 & -1.46 \\ 0.28 & 1.53 & 1.52 & 0.45 & -2.27 & 1.46 & 0.52 \\ 0.26 & -0.48 & -0.02 & 0.32 & 0.38 & -0.36 & 0.34 \\ -0.01 & -0.08 & 0.14 & 0.33 & -0.72 & 0.52 & -0.02 \\ -0.02 & 0.18 & -0.21 & 0.22 & 0.85 & 0.52 & -0.13 \end{bmatrix}$$

$$(J^T)_{\Sigma_j}^{\#} = \begin{bmatrix} 2.04 & 2.28 & -5.86 & 1.12 & 3.04 & -0.31 & 0.00 \\ 3.51 & -1.51 & -1.51 & -3.47 & -0.54 & 0.88 & -0.00 \\ 0.02 & 2.07 & 1.42 & 1.37 & -2.35 & 0.84 & 0.00 \\ 0.09 & -0.13 & -0.09 & 0.92 & 0.33 & -0.76 & 0.00 \\ -0.01 & -0.09 & 0.15 & 0.31 & -0.72 & 0.54 & -0.00 \\ 0.04 & 0.05 & -0.19 & -0.01 & 0.87 & 0.67 & -0.00 \end{bmatrix}$$

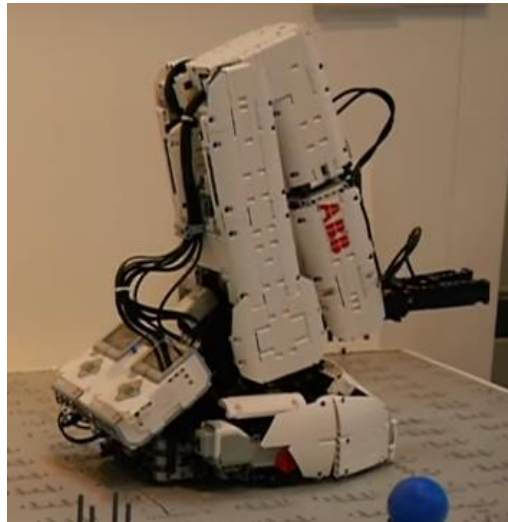


# You cannot measure everything – Conclusion

Increasing importance of models

## Drivers

- Performance demands
- Estimation and supervision
- Safety



More sensing  
→ more models needed  
(not less!)

Having models: good  
Knowing how much to trust them: better

(One) open question: What type  
of model for which purpose?



**ABB**